

# LES of propane-air swirling non-premixed flame using a SOM combustion model

## ARTICLE INFO

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*Non-premixed combustion is widely encountered in engine combustors. Large-eddy simulation (LES) was used to study non-premixed combustion by previous investigators using different combustion models. In this paper, the present authors used a second-order moment (SOM) combustion model for LES of propane-air swirling non-premixed combustion for the first time. The predicted time-averaged and RMS fluctuation velocities, time-averaged temperature and species concentration are in good agreement with experimental results, showing once again the feasibility of the SOM model. The instantaneous simulation results indicate that uniform temperature distribution was observed in most regions of the combustor, probably due to the annular fuel inlet and then an expansion to the combustor. The large-eddy vortex structures intensify swirling non-premixed combustion. Swirl thickens the flame front. Unlike the jet flame, no wrinkled flame front was observed in swirling non-premixed combustion.*

**Key words:** *swirling non-premixed propane-air flame, large-eddy simulation, second-order moment combustion model*

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## 1. Introduction

Non-premixed swirling turbulent flames are encountered in many kinds of combustors, such as gas-turbine engine combustors, internal combustion engines and furnace burners. Syred [17] summarized the principle, application, numerical and experimental studies on swirling flows and combustion. Khaleghi et al. [8] investigated an asymmetric non-premixed meso-scale swirling flame. The flame stability, heat loss, thermal efficiency and pollutant formation were compared with each other for different air-fuel inlet velocities and chemical equivalence ratios. Furthermore, the direct photography method was used to capture flame structures in a wide range of equivalence ratios in order to emphasize exceptional flame stability. Stöhr et al. [16] and Rehm et al. [12] studied the characteristics of an oscillating rotating turbulent diffusion flame using OH-PLIF and PIV techniques. The image information of OH radical fluorescence radiation intensity in the flame was obtained by PLIF, and the flame flow field was obtained by PIV. The combustion performance and flow field characteristics of turbulent flame were shown visually. Large-eddy simulation (LES) was used to study swirling flames. Different combustion models were used. Hu et al. [3] did LES using the fast-chemistry combustion models and PIV (particle image velocimetry) measurements of methane-air non-premixed combustion, and their studies were reviewed in [25]. Both LES and PIV results showed coherent structures of flames for different fuel-air ratios, but the LES statistical results for temperature and species concentration are only in qualitative agreement with the experimental results due to neglecting the reaction kinetics in the fast-chemistry combustion model. Navarro-Martinez [11] adopted a conditional moment closure (CMC) model to simulate non-premixed combustion. Some investigators used flame-let models for LES of non-premixed flames. Xing et al. [20] used the commercial software FLUENT to select a flame-generated manifolds (FGM) approach with detailed and reduced reaction mechanisms in a large eddy

simulation of a non-premixed methane-air jet flame (Sandia Flame D). Kempf et al. [7] used a flame-let model for LES of Sydney swirling non-premixed flames with different numerical methods. It was reported that the prediction results for combusting cases were not satisfactory. Zhu et al. [27] used a flame-let model in LES of non-premixed flame to study the local extinction. More complex models, like the PDF transport equation model was also used. Yang et al. [21] did a LES/PDF with an interaction-by-exchange with the mean (IEM) small-scale mixing model for non-premixed CO-H<sub>2</sub> jet flame and the LES results were well validated by direct numerical simulation (DNS). On the other hand, the thickened flame model was also used. Legier et al. [9] used a dynamically thickened flame model for LES of non-premixed combustion. Ke et al. [6] and Shang et al. [14] did LES of non-premixed methane-air combustion using a dynamically full thickened flame (DFTF) model and in comparison with a flame-let model. It was found that the two models gave similar results, but the DFTF can better catch the whole flame structures. Alternatively, the second-order moment (SOM) combustion model was proposed by Zhou et al. [24, 26] and was used in LES of non-premixed flames. Hu et al. [4] used the SOM combustion model for LES of swirling methane-air non-premixed flame, measured at Tsinghua University, and the Sydney swirling non-premixed flame [2]. It was found by comparison with experimental results that the SOM model is much better than the eddy-break-up (EBU) model, and swirling flames unlike the jet flame, do not have a wrinkled flame structure. Wang et al. [18] studied the Sandia methane-air jet non-premixed flame by large-eddy simulation using the SOM combustion model. Also, the SOM model gives good results. Ruihu and Teng [13] performed the LES of a methane/air co-axial jet non-premixed combustor coupled with flamelet generated manifolds (FGM) model, and the LES results were compared with experimental data. Yu et al. [22] did LES of Sandia turbulent non-premixed flame D, using both a

tabulated chemistry method coupled with three presumed probability density functions and a filtered density function (FDF) model. It was found that the latter is better. Wang et al. [19] did multi-regime mixing modeling for local extinction and re-ignition in turbulent non-premixed flame by using the LES/FDF method. Balabanov et al. [1] performed a differential subgrid stress model and its assessment in LES of non-premixed combustion. Recently Zhou et al. [24] used the SOM combustion model for LES of droplet-group combustion and found that combusting droplets reduces the drag force

It is seen that most LES of non-premixed swirling flames, including that using the SOM combustion model, were done for methane-air flames. In this paper, a large-eddy simulation is carried out for swirling propane-air non-premixed flame using the SOM combustion model for the first time. The experimental results for velocity, temperature, and species concentration assess the statistical results. The instantaneous simulation results are used to understand the flame structures.

## 2. Filtered govern equations for LES of turbulent flames and closure models

The filtered governing equations for LES of gas turbulent combustion can be given as [23]:

$$\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x_i} (\rho \bar{u}_i) = \bar{S} \quad (1)$$

$$\begin{aligned} & \frac{\partial}{\partial t} (\rho \bar{u}_i) + \frac{\partial}{\partial x_j} (\rho \bar{u}_i \bar{u}_j) = \\ & = \frac{\partial}{\partial x_j} \left( \mu \left( \frac{\partial \bar{u}_i}{\partial x_j} + \frac{\partial \bar{u}_j}{\partial x_i} \right) - \frac{2}{3} \left( \mu \frac{\partial \bar{u}_k}{\partial x_k} \right) \delta_{ij} \right) - \frac{\partial \bar{p}}{\partial x_i} + \\ & - \frac{\partial \tau_{sgs}}{\partial x_j} + \sum_k \frac{\rho_k}{\tau_{rk}} (\bar{u}_{ki} - u_i) + \bar{u}_i \bar{S} \end{aligned} \quad (2)$$

$$\begin{aligned} & \frac{\partial \rho \bar{Y}_s}{\partial t} + \frac{\partial}{\partial x_j} (\rho \bar{u}_j \bar{Y}_s) = \\ & = \frac{\partial}{\partial x_j} \left( \mu \frac{\partial \bar{Y}_s}{\partial x_j} \right) - \bar{w}_s - w_{sgs} - \frac{\partial g_{sgs}}{\partial x_j} + \alpha_s \bar{S} \end{aligned} \quad (3)$$

$$\begin{aligned} & \frac{\partial \rho \bar{h}}{\partial t} + \frac{\partial}{\partial x_j} (\rho \bar{u}_j \bar{h}) = \\ & = \frac{\partial}{\partial x_j} \left( \frac{\mu}{Pr} \frac{\partial \bar{h}}{\partial x_j} \right) - \bar{w}_s - \frac{\partial g_{sgs}}{\partial x_j} - q_r + S_h \end{aligned} \quad (4)$$

Here  $\tau_{sgs}$ ,  $g_{sgs}$ ,  $q_{sgs}$  and  $w_{sgs}$  denote sub-grid scale (SGS) stress, mass flux, heat flux and reaction rate respectively, needing to be closed. The SGS stress  $\tau_{sgs}$  is defined by

$$\tau_{sgs} = \rho \bar{u}_i \bar{u}_j - q \bar{u}_i \bar{u}_j \quad (5)$$

For the SGS stress, the Smagorinsky [15], Lilly [10] eddy-viscosity model is used as

$$\begin{aligned} \tau_{sgs} - \frac{1}{3} \tau_{kk} \delta_{ij} &= -2\mu_t \bar{S}_{ij}, \bar{S}_{ij} \equiv \frac{1}{2} \left( \frac{\partial \bar{u}_i}{\partial x_j} + \frac{\partial \bar{u}_j}{\partial x_i} \right) \\ \mu_t &= \rho L_s^2 |\bar{S}|, |\bar{S}| \equiv (2\bar{S}_{ij} \bar{S}_{ij})^{1/2} \end{aligned} \quad (6)$$

where  $L_s = \min(\kappa d, C_s V^{1/3})$ . The sub-grid scale mass flux and heat flux are closed by gradient modelling.

$$g_{sgs} = \rho (\bar{u}_j \bar{Y}_s - \bar{u}_j \bar{Y}_s) = \frac{\mu_t}{\sigma_Y} \frac{\partial \bar{Y}_s}{\partial x_j} \quad (7)$$

$$q_{sgs} = \rho (\bar{u}_j \bar{T} - \bar{u}_j \bar{T}) = \frac{\mu_t}{\sigma_T} \frac{\partial \bar{T}}{\partial x_j} \quad (8)$$

where  $\sigma_Y$  and  $\sigma_T$  are model constants, taken as  $\sigma_Y = \sigma_T = 1.0$ .

The SGS reaction rate were closed using a second-order moment (SOM) combustion model, proposed by Zhou et al. [23, 26]. The instantaneous Arrhenius expression of the chemical reaction rate of a global one-step reaction is

$$w_s = B \rho^2 Y_{fu} Y_{ox} \exp\left(-\frac{E}{RT}\right) \quad (9)$$

The filtered reaction rate is

$$\bar{w}_s = \rho^2 \bar{K} \bar{Y}_{ox} \bar{Y}_{fu}, \bar{K} = B \int \exp\left(-\frac{E}{RT}\right) p(\bar{T}) d\bar{T} \quad (10)$$

The SOM-SGS combustion model, using a gradient modeling and expressing the effect of small-scale temperature and species fluctuations on the SGS reaction rate, is given by

$$\begin{aligned} w_{sgs} &= \rho^2 [\bar{K} (\bar{Y}_{ox} \bar{Y}_{fu} - \bar{Y}_{ox} \bar{Y}_{fu}) + \bar{Y}_{ox} (\overline{K Y_{fu}} - \bar{Y}_{fu} \bar{K}) + \\ & + \bar{Y}_{fu} (\overline{K Y_{ox}} - \bar{Y}_{ox} \bar{K})] \end{aligned} \quad (11)$$

The sub-grid scale correlation terms are given by the following algebraic expression

$$\overline{\Phi \Psi} - \bar{\Phi} \bar{\Psi} = c \mu_t \left( \frac{\partial \bar{\Phi}}{\partial x_j} \right) \left( \frac{\partial \bar{\Psi}}{\partial x_j} \right) / \rho / \left( \frac{a}{\tau_T} + \frac{1-a}{\tau_c} \right) \quad (12)$$

where  $\Phi$  and  $\Psi$  denote  $Y_1$  or  $Y_2$  or  $K$ , and  $\tau_c$  is the chemical reaction time,  $\tau_T$  is the turbulent diffusion time,  $a$  and  $c$  are model constants, taken as  $a = 0.9$  and  $c = 0.5$ . The reaction time and fluctuation time are given by

$$\tau_c = \left[ B \rho (\bar{Y}_{O_2} + \beta \bar{Y}_{CH_4}) \exp\left(-\frac{E}{RT}\right) \right], \tau_T = \frac{1}{|\bar{S}|}$$

where  $\beta$  is the stoichiometric coefficient.

For the propane-oxygen reaction rate, the global one-step reaction rate is adopted:

$$w_{C_3H_8} = 4.79 \cdot 10^8 \rho^{1.75} Y_{C_3H_8}^{0.1} Y_{O_2}^{0.65} \exp\left(-1.51 \cdot \frac{10^4}{T}\right) \quad (13)$$

For the radiative heat transfer, the PI model was used.

## 3. Simulated combustor and numerical procedure

The simulated propane-air swirling non-premixed flame was taken in a swirl combustor with an annular fuel inlet, measured in [5]. The geometrical configuration and sizes of the swirl combustor to be predicted are given in Fig. 1 and Table 1. The inlet-flow parameters are given in Table 2.

The swirl number is 0.78; the wall temperature is taken as 1373 K. The grid sizes in  $x$ ,  $y$  and  $z$  directions are 1–2 mm. The total number of cells is 450,000. The grid arrangement is shown in Fig. 2. The time step is taken as 0.005 s. The convergence can be reached within each time step after 10 to 20 iterations. For the numerical procedure, the pressure-implicit split-operator (PISO) algorithm was used for  $p$ - $v$  corrections, the second order implicit difference scheme for the time-dependent term, and the central differencing difference scheme for the convection and diffusion terms were adopted. The boundary condition

at the exit is based on a fully developed flow assumption where the gradients for all flow variables in the axial direction are zero. At the near-wall grid nodes, the wall function approximation was employed.

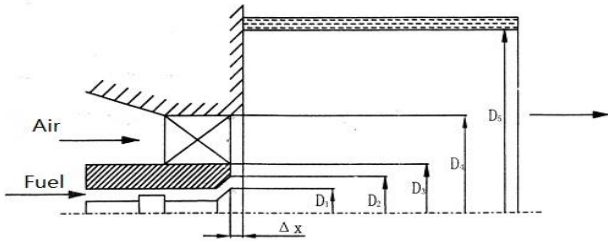


Fig. 1. A swirl combustor

Table 1. Geometrical sizes

D <sub>1</sub> [mm]	D <sub>2</sub> [mm]	D <sub>3</sub> [mm]	D <sub>4</sub> [mm]	D <sub>5</sub> [mm]	L [mm]
17	19	21	42	100	300

Table 2. Flow parameters

	Mass flow rate [kg/s]	Axial velocity [m/s]	Radial velocity [m/s]	Tangential velocity [m/s]	Temperature [K]
Fuel inlet	$1.284 \cdot 10^{-3}$	12.43	12.43	—	294
Air inlet	$30.4 \cdot 10^{-3}$	25.96	—	25.96	313

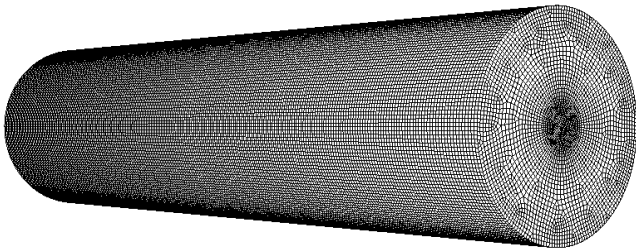


Fig. 2. Grid arrangement

#### 4. Time-averaged simulation results and their experimental validation

The obtained time-averaged temperature, axial and tangential velocities (where  $u_{av}$  denotes the averaged inlet velocity), axial and tangential RMS fluctuation velocities, propane, CO<sub>2</sub> and oxygen volume fractions, validated by experimental results are shown in Fig. 3 to 10.

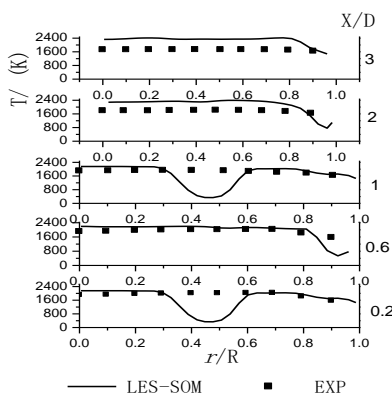


Fig. 3. Time-averaged temperature

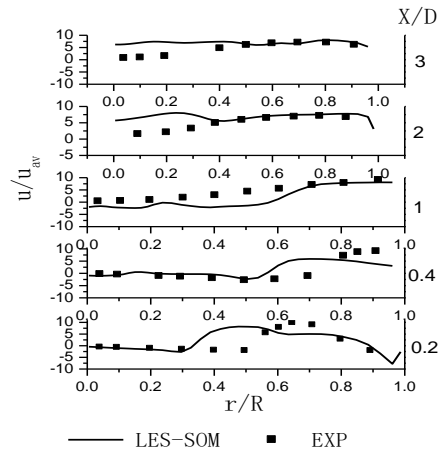


Fig. 4. Time-averaged axial velocity

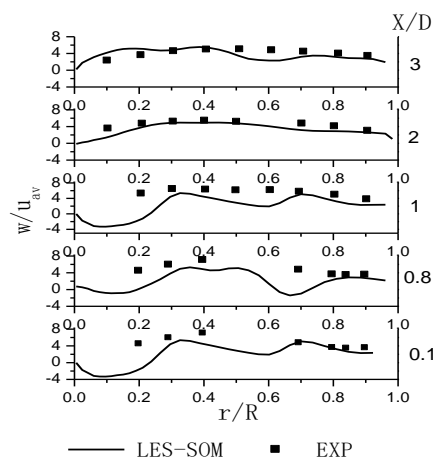


Fig. 5. Time-averaged tangential velocity

It is seen that in most regions the agreement between predictions and measurements is good. Some discrepancies between predictions and experiments are caused possibly due the assumption of uniform velocity, temperature and species concentration distributions at the inlet, but actually these distributions are non-uniform.

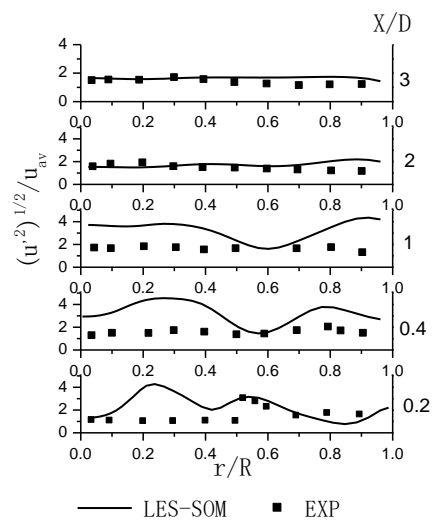


Fig. 6. Axial RMS fluctuation velocity

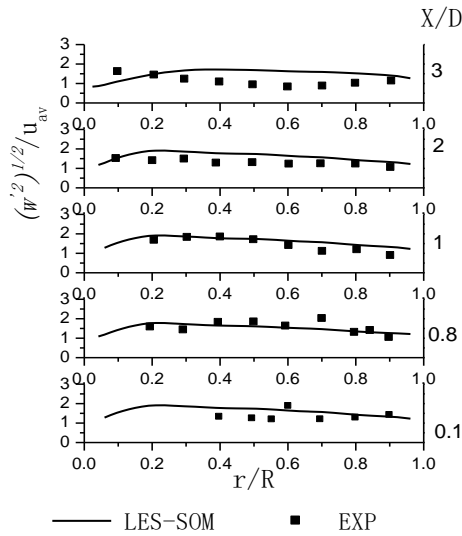


Fig. 7. Tangential RMS fluctuation velocity

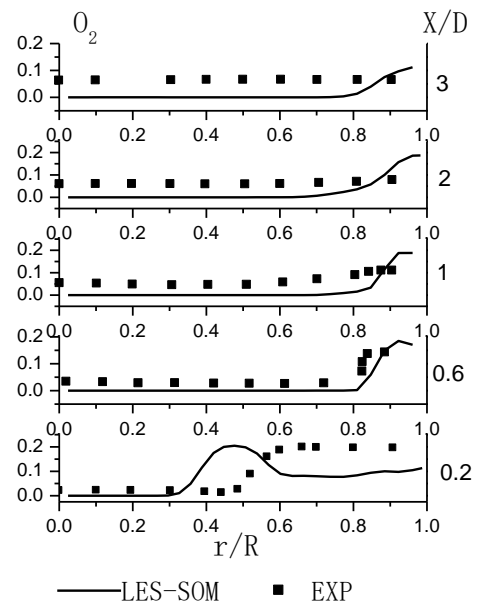


Fig. 10. Oxygen volume fraction

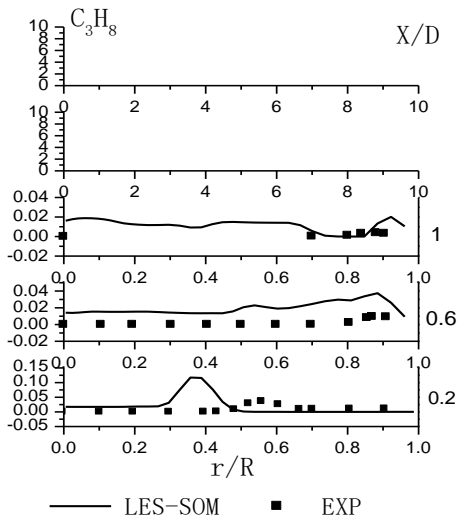


Fig. 8. Propane volume fraction

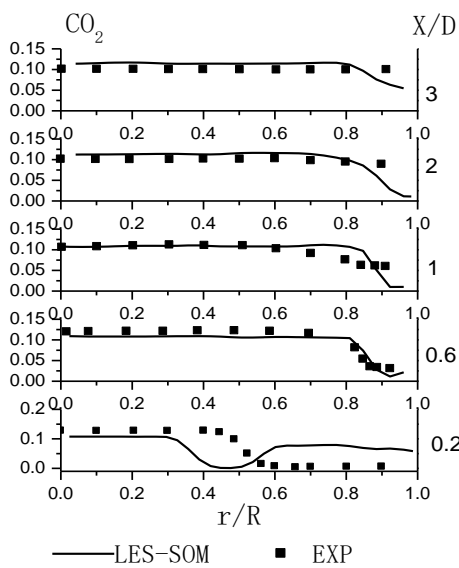
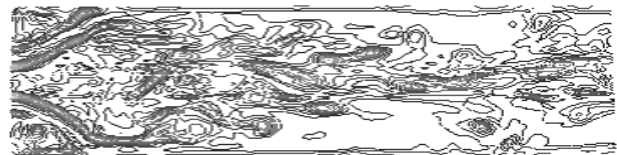


Fig. 9. CO<sub>2</sub> volume fraction

### 5. Instantaneous flame structures

Figures 11 and 12 give the instantaneous vorticity isolines in the  $r$ - $z$  planes at  $\theta = 90^\circ$  and  $\theta = 0^\circ$ , and in the  $r$ - $\theta$  planes at  $z = 40$  mm, 100 mm and 250 mm respectively. The large-size vortices are at first produced near the inlet shear region and then spread to the central region. Stronger turbulence exists in these regions. The oncoming flow from the annular inlets forms a large shear layer. Many small vortices are formed around the shear layer. The shear layer diffuses quickly; the vorticity is largest near the inlet and the large vortex structures formed in the upstream region are quickly broken up.

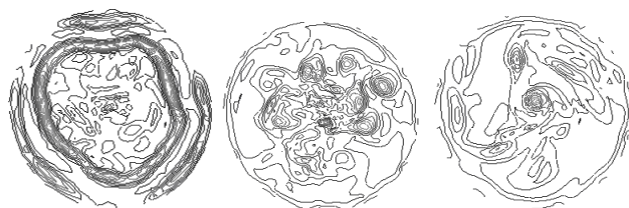


a)  $r$ - $z$  plane,  $\theta = 0^\circ$



b)  $r$ - $z$  plane,  $\theta = 90^\circ$

Fig. 11. Instantaneous vorticity isolines



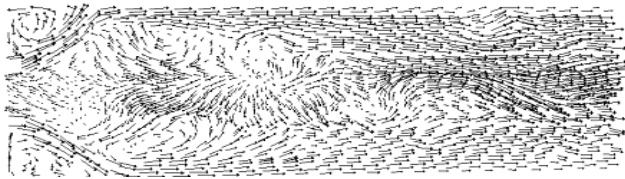
a)  $z = 40$  mm

b)  $z = 100$  mm

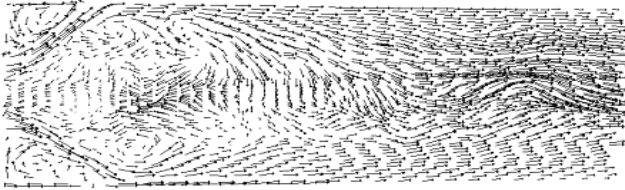
c)  $z = 250$  mm

Fig. 12. Instantaneous vorticity isolines ( $r$ - $\theta$  plane)

Figures 13 and 14 show the instantaneous velocity vectors in the  $r$ - $z$  and  $r$ - $\theta$  planes, respectively. There are two corner recirculation and many central recirculation zones, indicating the complex structure of the flow field.

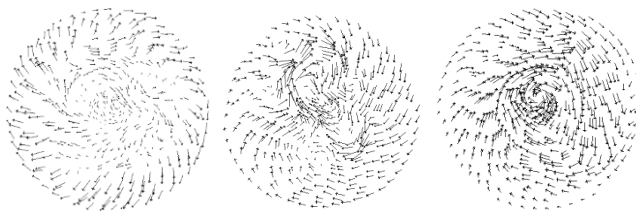


a)  $r$ - $z$  plane,  $\theta = 0^\circ$



b)  $r$ - $z$  plane,  $\theta = 90^\circ$

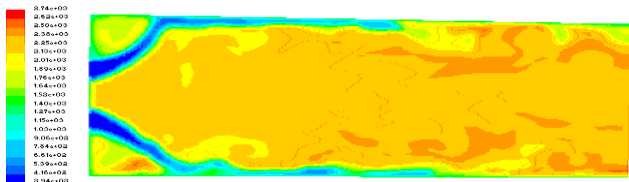
Fig. 13. Instantaneous velocity vectors



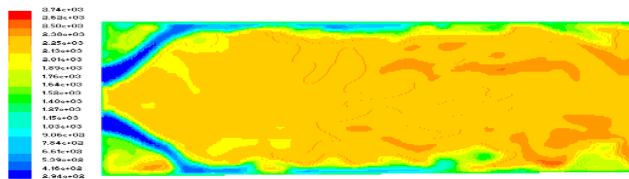
a)  $z = 40$  mm      b)  $z = 100$  mm      c)  $z = 250$  mm

Fig. 14. Instantaneous velocity vectors ( $r$ - $\theta$  planes)

Figures 15 to 20 give obtained instantaneous temperature, propane and oxygen mass fraction maps in the  $r$ - $z$  planes at  $\theta = 90$  and  $\theta = 0^\circ$ , and in the  $r$ - $\theta$  planes at  $z = 40$  mm, 100 mm and 250 mm respectively. It is seen that the temperature distribution is rather uniform, because the fuel is supplied from an annular inlet and then discharged with an angle of expansion.



a)  $r$ - $z$  plane,  $0^\circ$



b)  $r$ - $z$  plane,  $90^\circ$

Fig. 15. Instantaneous temperature maps

This case is different from the central supply of fuel in other swirl combustors. High temperature develops immediately behind the inlet shear region. The chemical reaction is intensified by the large-eddy structures in swirling flows. Unlike the jet flame, there is no distinct thin flame surface (wrinkled flame structure) in the swirling flame. This implies that the swirl thickens the flame front. Propane and oxygen were rapidly exhausted behind the inlet region, but some residual oxygen remains in the near-wall region, showing that combustion intensively takes place in most regions of the combustor.

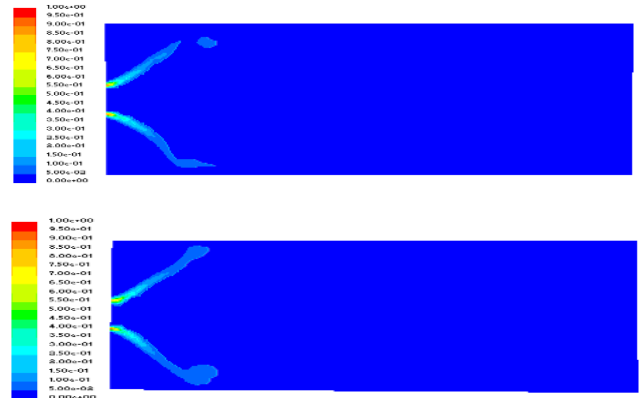


Fig. 16. Instantaneous propane mass fraction maps (top,  $r$ - $z$  plane,  $0^\circ$ ) (bottom,  $r$ - $z$  plane,  $90^\circ$ )

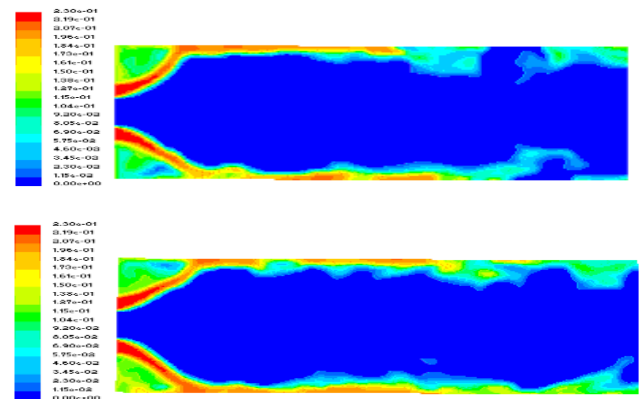


Fig. 17. Instantaneous oxygen mass fraction maps (top,  $r$ - $z$  plane,  $0^\circ$ ) (bottom,  $r$ - $z$  plane,  $90^\circ$ )

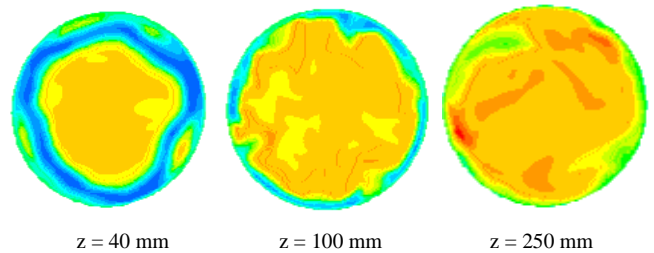
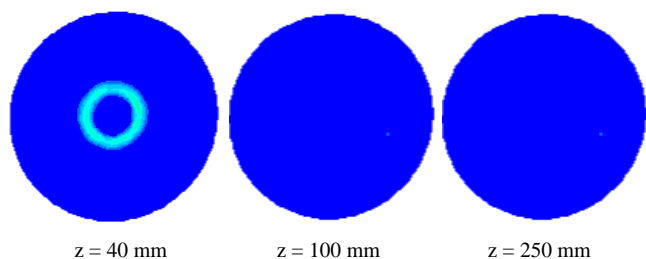
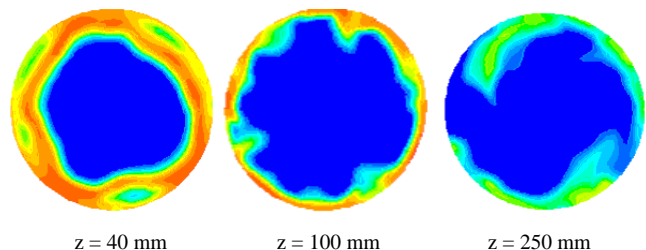


Fig. 18. Instantaneous temperature maps ( $r$ - $\theta$  plane)

Fig. 19. Instantaneous propane mass fraction maps ( $r$ - $\theta$  plane)Fig. 20. Instantaneous oxygen mass fraction maps ( $r$ - $\theta$  plane)

## Conclusions

1. The swirling propane-air non-premixed combustion was studied by large-eddy simulation using a second-order

moment (SOM) combustion model. The statistical results for time-averaged temperature, species concentration, time-averaged and RMS fluctuation velocities were well validated by experimental results, indicating that the simulation results are reliable and the SOM combustion model is good for simulating complex turbulent flames.

2. A complex flow structures with many large-scale structures produced by the highly shear near the inlet were observed, where strong turbulence is located.
3. Uniform temperature distribution was observed in most regions of the combustor, probably due to the annular fuel inlet and then an expansion to the combustor.
4. The large-eddy vortex structures intensify swirling non-premixed combustion. Swirl thickens the flame front.
5. Unlike the jet flame, no wrinkled flame front was observed in swirling non-premixed combustion.
6. Multiple and detailed reaction mechanisms are needed instead of the one-step global reaction mechanism in the SOM combustion model.

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